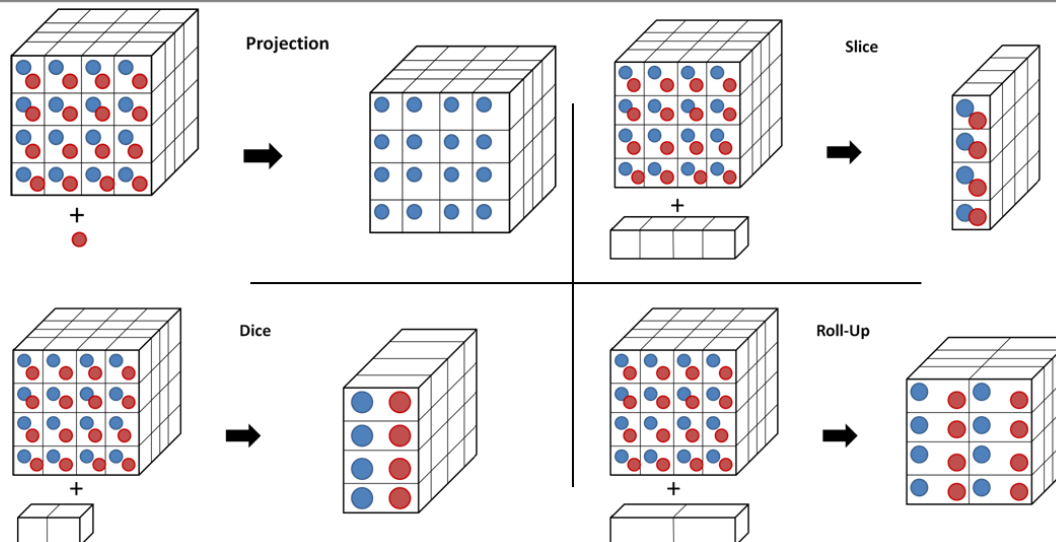


# Interacting with Statistical Linked Data via OLAP Operations

Benedikt Kämpgen, Seán O’Riain, Andreas Harth

International Workshop on Interacting with Linked Data, Extended Semantic Web Conference 2012  
28 May 2012

Institute of Applied Informatics and Formal Description Methods (AIFB)



# Outline

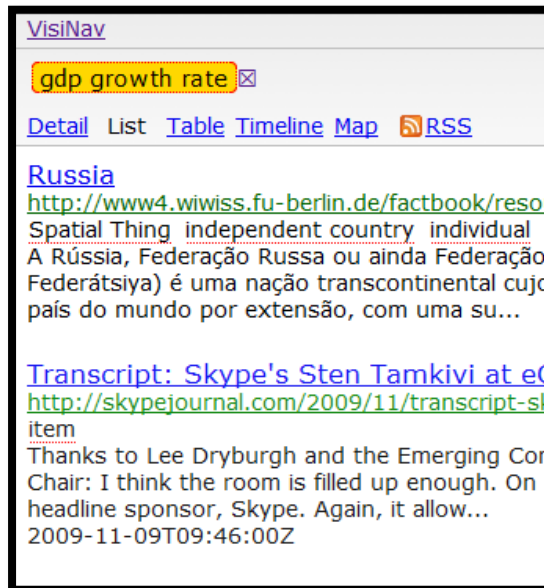
- Interacting with Statistical Linked Data
- Data Cubes as RDF
- OLAP Operations and Queries
- OLAP Queries in SPARQL
- Evaluation/Discussion/Conclusions

# Outline

- **Interacting with Statistical Linked Data**
- Data Cubes as RDF
- OLAP Operations and Queries
- OLAP Queries in SPARQL
- Evaluation/Discussion/Conclusions

# Decision Support using Statistical Linked Data

Difficulties with statistics as Linked Data:  
**No aggregation, spreadsheets and pivot tables, or drill-down.**



VisiNav

gdp growth rate

Detail List Table Timeline Map RSS

Russia

<http://www4.wiwiwiss.fu-berlin.de/factbook/reso>

Spatial Thing independent country individual

A Rússia, Federação Russa ou ainda Federação Federátsiya) é uma nação transcontinental cujo país do mundo por extensão, com uma su...

Transcript: Skype's Sten Tamkivi at eC

<http://skypejournal.com/2009/11/transcript-sk>

item

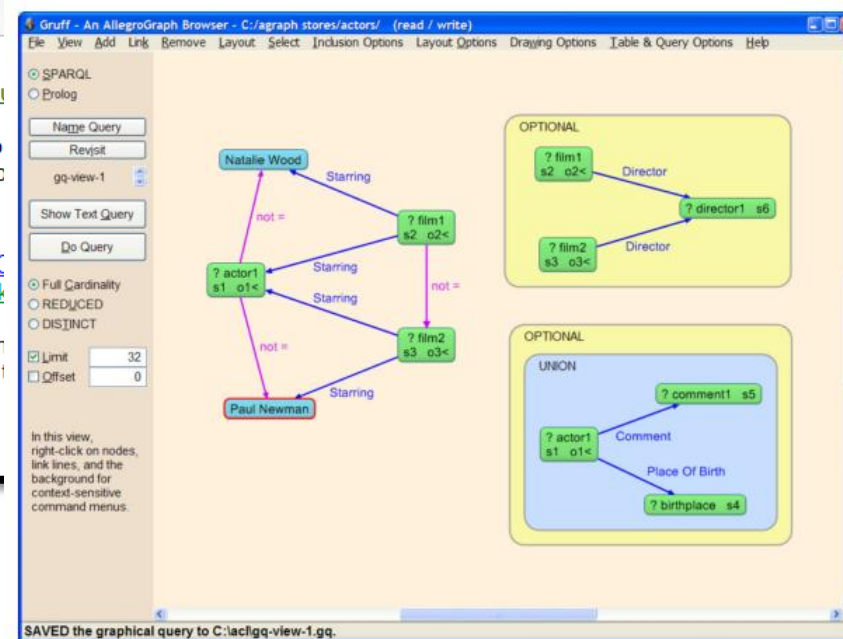
Thanks to Lee Dryburgh and the Emerging Cor

Chair: I think the room is filled up enough. On

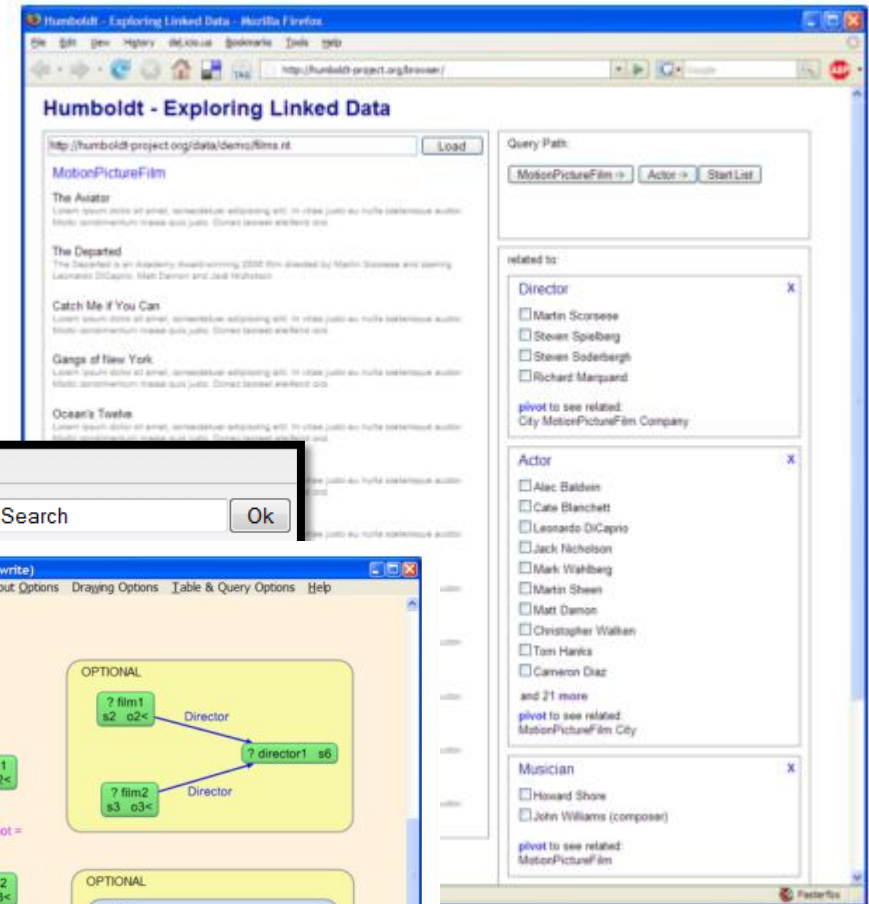
headline sponsor, Skype. Again, it allow...

2009-11-09T09:46:00Z

Visinav Linked Data  
browser [1]



Gruff SPARQL query builder [2]



Humboldt - Exploring Linked Data - Mozilla Firefox

http://humboldt-project.org/data/demos/films.rst

Load

MotionPictureFilm

The Aviator

The Departed

Catch Me if You Can

Gangs of New York

Ocean's Twelve

Query Path:

MotionPictureFilm Actor StartList

related to:

Director

Martin Scorsese

Steven Spielberg

Steven Soderbergh

Richard Marquand

pivot to see related:

City MotionPictureFilm Company

Actor

Alec Baldwin

Cate Blanchett

Leonardo DiCaprio

Jack Nicholson

Mark Wahlberg

Martin Sheen

Matt Damon

Christopher Walken

Tam Hanks

Cameron Diaz

and 21 more

pivot to see related:

MotionPictureFilm City

Musician

Howard Shore

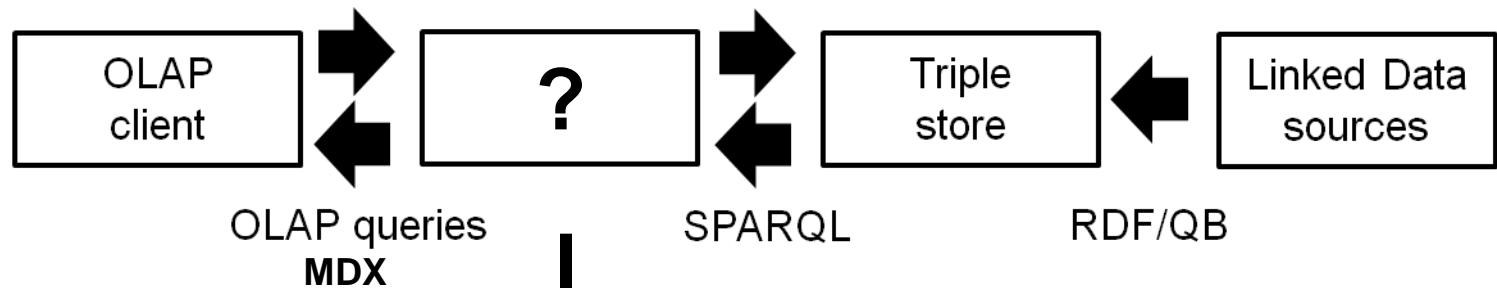
John Williams (composer)

pivot to see related:

MotionPictureFilm

Humboldt faceted  
search [3]

# Online Analytical Processing of Statistical Linked Data



- Typical OLAP client
- OLAP operations
- OLAP queries
- Multidimensional Expression Language (MDX)

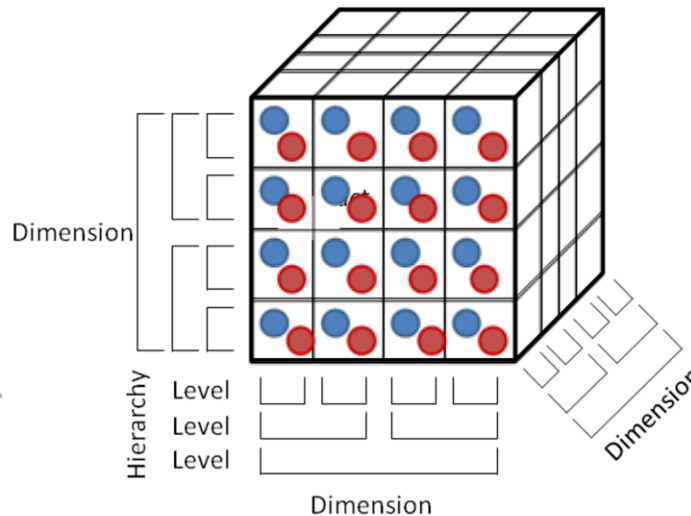
- Statistical Linked Data re-using the RDF Data Cube Vocabulary (QB)
- Crawled into triple store
- SPARQL endpoint



Problem: How to map MDX queries to SPARQL queries?

# Scenario

Financial data about US companies as RDF in triple store



**Data cube:** Financial disclosures

**Measures:** Cost of goods sold, Sales (UDF aggr. funct.)

**Dimensions:** Issuer, Dtstart, Dtend, Segment



**OLAP query**

*Pivot table*

Columns (issuer)		RAYONIER INC	WEYERHAEUSER CO
Rows (dtstart, dtend)			
2009-01-01	2009-3-31	1,100,335 USD	0 values
2009-04-01	2009-06-30	2 values	2,300,800 USD
...	...	...	...

Filters: CostOfGoodsSold

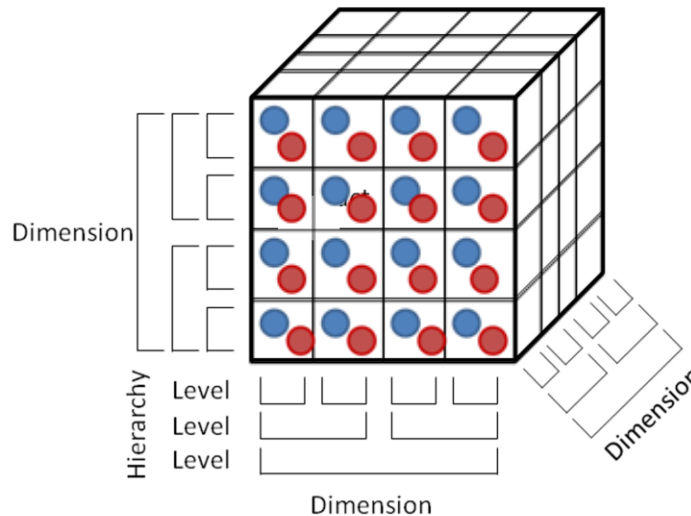


<http://diveintechno.com/information-technology-business-analyst.html>

Business analyst  
with  
OLAP client

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Financial data about US companies as RDF in triple store



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...	...	...	...

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# Approach - Overview

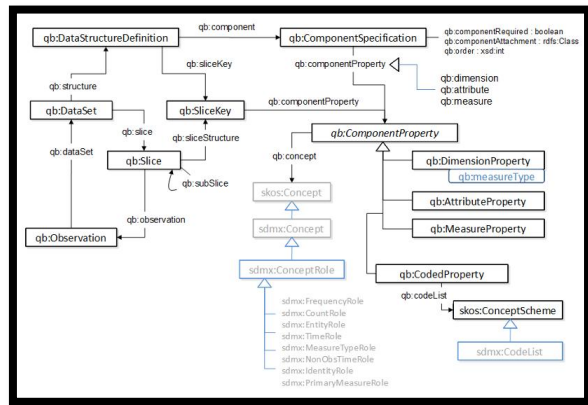
1. **Data cubes** mapped to RDF re-using QB
2. **OLAP operations** with data cubes as input/output
3. **OLAP queries** as sets of OLAP operations on data cubes
4. **SPARQL queries** from OLAP queries



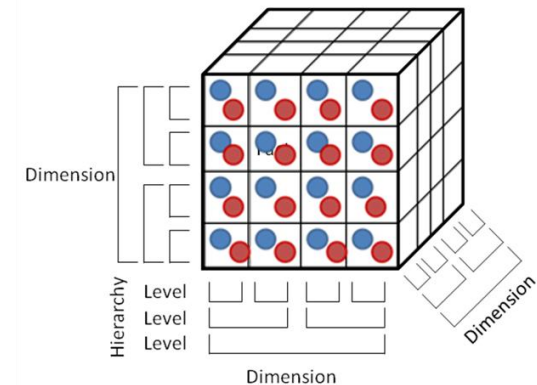
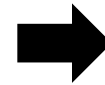
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- Interacting with Statistical Linked Data
- **Data Cubes as RDF**
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# Data Cubes as RDF (1)



The RDF Data Cube Vocabulary [4]



Common Data Cube Model

**DataCubeSchema** defines the set of data cube schemas as  $\{(?x, D, M) \in (\mathcal{I} \cup \mathcal{B}) \times \mathcal{D} \times \mathcal{M} \mid (?x \text{ a } qb:DataSetDefinition \wedge \forall d \in D (?x \text{ qb:componentProperty } ?comp \wedge ?comp \text{ qb:dimensionProperty } iri(d)) \wedge \forall m \in M (?x \text{ qb:componentProperty } ?comp \wedge ?comp \text{ qb:measureProperty } iri(m)))\}$ .

**DataCube** defines the set of data cubes as  $DataCube = \{(cs, F) \in DataCubeSchema \times \mathcal{F} \mid cs = (?x, D, M) \wedge D = \{D_0, \dots, D_{|D|}\} \wedge M = \{m_0, \dots, m_{|M|}\} \wedge \forall c \in F (c = (?obs, c_0, \dots, c_{|D|}, e_0, \dots, e_{|M|}) : (?obs \text{ qb:dataset } ?ds \wedge ?ds \text{ qb:structure } ?x) \wedge \forall D_i \in D (?obs \text{ iri}(D_i) c_i \wedge iri(D_i) \text{ qb:codeList } ?h \wedge ?l \text{ skos:inScheme } ?h \wedge ?v \text{ skos:member } ?l \wedge (?v \text{ skos:notation } ?c_i \vee ?v \text{ skos:exactMatch } ?c_i)) \wedge \forall m_i \in M (?obs \text{ iri}(m_i) e_i \vee e_i = null))\}$ .

# Data Cubes as RDF (2)

## Scenario

- Cube URIs:
  - `edgar:SecCubeGrossProfitMargin`
- Dimension URIs:
  - `edgar:issuer`
  - `edgar:dtstart`
  - `edgar:dtend`
  - `edgar:segment`
- Measure URIs:
  - `edgar:CostOfGoodsSold`
  - `edgar:sales`

# Materialising Data Cubes

- Computing all possible facts of a data cube (materialisation) requires  $2^{|D|}$  subqueries [5].

Issuer	Dtstart	Dtend	Segment	COGS	Sales
RAYONIER INC	2009-01-01	2009-03-31	Business	1,100,335 USD	2,000,000
RAYONIER INC	2009-04-01	2009-06-30	Business	500,442 USD	1,245,000
...	...	...	...	...	...
RAYONIER INC	2009-01-01	2009-03-31	ALL	1,100,335 USD	2,000,000
...	...	...	...	...	...
...	...	ALL	...	...	...
...	...	...	...	...	...
...	ALL	...	...	...	...
...	...	...	...	...	...
ALL	...	...	...	...	...
...	...	...	...	...	...
...	...	ALL	ALL	...	...
...	...	...	...	...	...
ALL	ALL	ALL	ALL	...	...

**Scenario:** Financial disclosure: Issuer (625), Dtstart (27), Dtend (20), Segment (21,227) has **7,813,772** possible facts.

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RAYONIER INC	2009-01-01	2009-03-31	ALL	1,100,335 USD	2,000,000
...	...	...	...	...	...
...	...	ALL	...	...	...
...	...	...	...	...	...
...	ALL	...	...	...	...
...	...	...	...	...	...
ALL	...	...	...	...	...
...	...	...	...	...	...
...	...	ALL	ALL	...	...
...	...	...	...	...	...
ALL	ALL	ALL	ALL	...	...

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...	...	...	...	...	...
...	...	ALL	...	...	...
...	...	...	...	...	...
...	ALL	...	...	...	...
...	...	...	...	...	...
ALL	...	...	...	...	...
...	...	...	...	...	...
...	...	ALL	ALL	...	...
...	...	...	...	...	...
ALL	ALL	ALL	ALL	...	...

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...	...	...	...	...	...
...	...	ALL	...	...	...
...	...	...	...	...	...
...	ALL	...	...	...	...
...	...	...	...	...	...
ALL	...	...	...	...	...
...	...	...	...	...	...
...	...	ALL	ALL	...	...
...	...	...	...	...	...
ALL	ALL	ALL	ALL	...	...

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...	...	...	...	...	...
...	...	ALL	...	...	...
...	...	...	...	...	...
...	ALL	...	...	...	...
...	...	...	...	...	...
ALL	...	...	...	...	...
...	...	...	...	...	...
...	...	ALL	ALL	...	...
...	...	...	...	...	...
ALL	ALL	ALL	ALL	...	...

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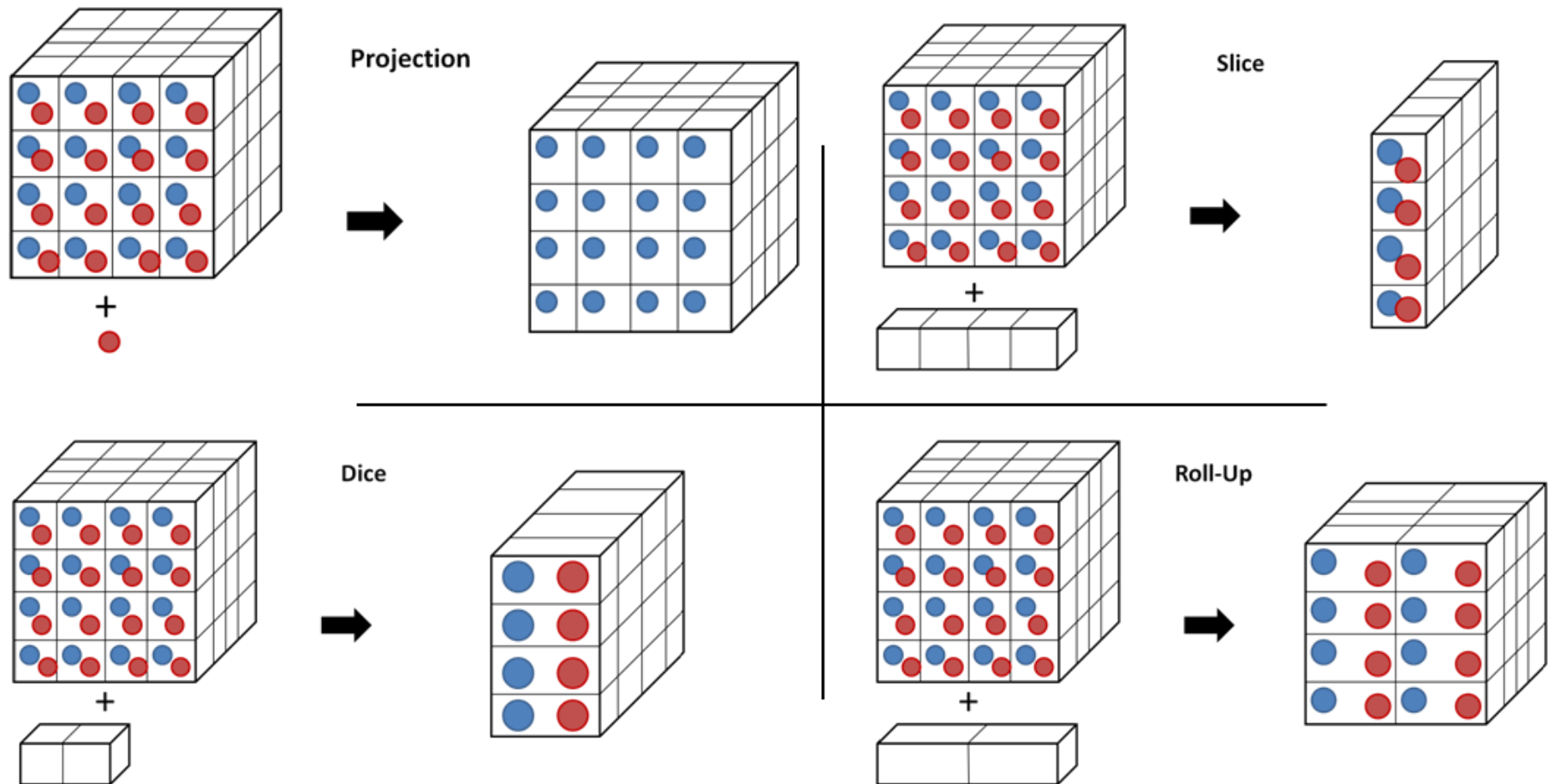
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...	...	...	...	...	...
...	...	ALL	...	...	...
...	...	...	...	...	...
...	ALL	...	...	...	...
...	...	...	...	...	...
ALL	...	...	...	...	...
...	...	...	...	...	...
...	...	ALL	ALL	...	...
...	...	...	...	...	...
ALL	ALL	ALL	ALL	...	...

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# OLAP Operations – Informal



# OLAP Operations – Formal

**Projection** is defined as  $Projection : DataCube \times Measure \rightarrow DataCube$  and removes a measure from the input cube and allows to query only for specific measures. We evaluate *Projection* by removing a measure from the subcube query tuple.

**Slice** is defined as  $Slice : DataCube \times Dimension \rightarrow DataCube$  and removes a dimension from the input cube and aggregates over the members of a dimension. We evaluate *Slice* by setting the tuple element of that dimension to *ALL*.

Dice, Roll-Up (see paper)

- Input/Output: data cubes; OLAP operations can be nested.
- Nested set of OLAP operations on data cube lead to OLAP query.
- OLAP query returns subset of facts in materialised data cube.

# Scenario

OLAP operations:

- 1)  $Q = \text{Projection}(\text{edgar:SecCubeGrossProfitMargin}, \text{ed:sales})$
- 2)  $Q = \text{slice}(Q, \text{ed:Segment})$



Issuer	Dtstart	Dtend	Segment	COGS
RAYONIER INC	2009-01-01	2009-03-31	ALL	1,100,335 USD
RAYONIER INC	2009-04-01	2009-06-30	ALL	500,442 USD
...	...	...	...	...
RAYONIER INC	2009-01-01	2009-03-31	ALL	1,100,335 USD
...	...	...	...	...

# OLAP Queries

## OLAP query (subcube query)

$(q_0, \dots, q_{|D|}, m_0, \dots, m_{|M|})$  with  $\text{dom}(q_i) = \{?, ALL, x\}$  with  $?$  for an inquired dimension, with  $ALL$  for an aggregated dimension, with  $x$  for one or more members to fix a dimension, and with  $m_i$  a measure to query for.

## Scenario

$(?, ?, ?, ?, \text{COGS}, \text{Sales})$

Full-cube query: All explicitly contained facts in a data cube.

$(\{\text{RAYONIER INC}\}, \{2009-01-01\}, \{2009-03-31\}, \{\text{Business}\}, \text{COGS}, \text{Sales})$

Point query: One specific explicitly contained fact from a data cube.

$(ALL, ALL, ALL, ALL, \text{COGS}, \text{Sales})$

Fully-aggregated query: Implicitly contained fact aggregating over all dimensions.

# OLAP Queries as Sets of OLAP operations on a Data Cube

**Projection** is defined as  $Projection : DataCube \times Measure \rightarrow DataCube$  and removes a measure from the input cube and allows to query only for specific measures. We evaluate *Projection* by removing a measure from the subcube query tuple.

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Dice, Roll-Up (see paper)

## Scenario

OLAP operations:

- 1)  $Q = Projection(edgar:SecCubeGrossProfitMargin, edgar:Sales)$
- 2)  $Q = slice(Q, edgar:Segment)$



OLAP query:

- Init)  $Q = (?, ?, ?, ?, Cost\ of\ goods\ sold, Sales)$
- 1)  $Q = (?, ?, ?, ?, Cost\ of\ goods\ sold)$
  - 2)  $Q = (?, ?, ?, ALL, Cost\ of\ goods\ sold)$

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# OLAP Queries in SPARQL

- Given a **subcube query**, resulting from a set of nested OLAP operations on a data cube:

$$Q = (q_0, \dots, q_{|D|}, m_0, \dots, m_{|M|})$$

- Translated into SPARQL query:
  1. Initial SPARQL query for all facts from the data cube.
  2. For each selected measure, add aggregated selection and graph pattern.
  3. For each inquired dimension, add selection, graph patterns, and group by.
  4. For each fixed dimension, add graph pattern.

# Scenario

1.

**1. Initial  
SPARQL  
query for all  
facts from the  
data cube.**

```
select ?dimMem0 ?dimMem1 ?dimMem2 count(xsd:decimal(?  
    measureValue0)) sum(xsd:decimal(?measureValue0))  
where {  
    ?obs qb:dataSet ?ds.  
    ?ds qb:structure edgar:SecCubeGrossProfitMargin.  
    ?obs edgar:issuer ?values0.  
        ?dimMem0 skos:member ?level0.  
        ?level0 skos:inScheme ?hierarchy0.  
        edgar:issuer qb:codeList ?hierarchy0.  
        ?dimMem0 skos:exactMatch ?values0.  
    ?obs edgar:dtstart ?values1.  
        ?dimMem1 skos:member ?level1.  
        ?level1 skos:inScheme ?hierarchy1.  
        edgar:dtstart qb:codeList ?hierarchy1.  
        ?dimMem1 skos:notation ?values1.  
    ?obs edgar:dtend ?values2.  
        ?dimMem2 skos:member ?level2.  
        ?level2 skos:inScheme ?hierarchy2.  
        edgar:dtend qb:codeList ?hierarchy2.  
        ?dimMem2 skos:notation ?values2.  
    ?obs edgar:CostOfGoodsSold ?measureValue0.  
} group by ?dimMem0 ?dimMem1 ?dimMem2
```

SPARQL query translated from subcube query

## 2.1 Scenario

2. For each selected measure, add aggregated selection and graph pattern.

```
select ?dimMem0 ?dimMem1 ?dimMem2 count(xsd:decimal(?
    measureValue0)) sum(xsd:decimal(?measureValue0))
where {
  ?obs qb:dataSet ?ds.
  ?ds qb:structure edgar:SecCubeGrossProfitMargin.
  ?obs edgar:issuer ?values0.
    ?dimMem0 skos:member ?level0.
    ?level0 skos:inScheme ?hierarchy0.
    edgar:issuer qb:codeList ?hierarchy0.
    ?dimMem0 skos:exactMatch ?values0.
  ?obs edgar:dtstart ?values1.
    ?dimMem1 skos:member ?level1.
    ?level1 skos:inScheme ?hierarchy1.
    edgar:dtstart qb:codeList ?hierarchy1.
    ?dimMem1 skos:notation ?values1.
  ?obs edgar:dtend ?values2.
    ?dimMem2 skos:member ?level2.
    ?level2 skos:inScheme ?hierarchy2.
    edgar:dtend qb:codeList ?hierarchy2.
    ?dimMem2 skos:notation ?values2.
  ?obs edgar:CostOfGoodsSold ?measureValue0.
} group by ?dimMem0 ?dimMem1 ?dimMem2
```

SPARQL query translated from subcube query

## 3.1 Scenario

3. For each inquired dimension, add selection, graph patterns, and group by.

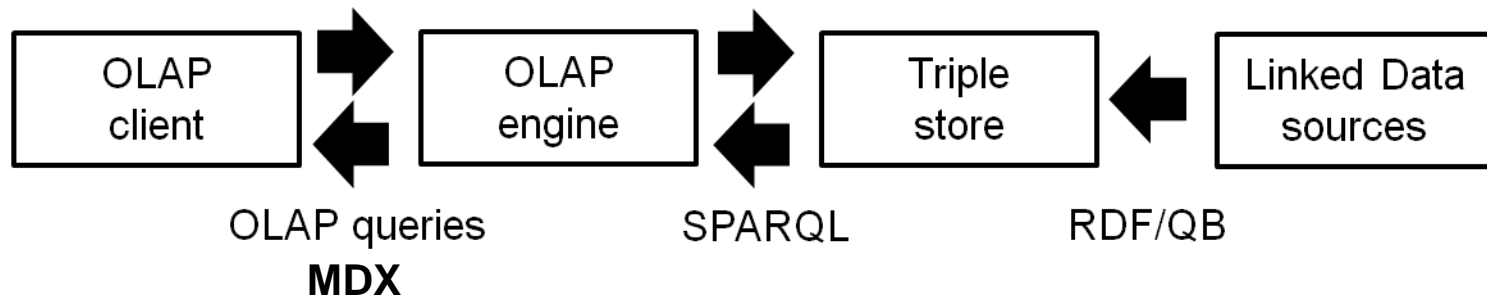
```
select ?dimMem0 ?dimMem1 ?dimMem2 count(xsd:decimal(?
    measureValue0)) sum(xsd:decimal(?measureValue0))
where {
  ?obs qb:dataSet ?ds.
  ?ds qb:structure edgar:SecCubeGrossProfitMargin.
  ?obs edgar:issuer ?values0.
    ?dimMem0 skos:member ?level0.
    ?level0 skos:inScheme ?hierarchy0.
    edgar:issuer qb:codeList ?hierarchy0.
    ?dimMem0 skos:exactMatch ?values0.
  ?obs edgar:dtstart ?values1.
    ?dimMem1 skos:member ?level1.
    ?level1 skos:inScheme ?hierarchy1.
    edgar:dtstart qb:codeList ?hierarchy1.
    ?dimMem1 skos:notation ?values1.
  ?obs edgar:dtend ?values2.
    ?dimMem2 skos:member ?level2.
    ?level2 skos:inScheme ?hierarchy2.
    edgar:dtend qb:codeList ?hierarchy2.
    ?dimMem2 skos:notation ?values2.
  ?obs edgar:CostOfGoodsSold ?measureValue0.
} group by ?dimMem0 ?dimMem1 ?dimMem2
```

SPARQL query translated from subcube query

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# Evaluation/Discussion



## Scenario

- OLAP query took 18sec and returned 58 facts to be filled into the requested pivot table.

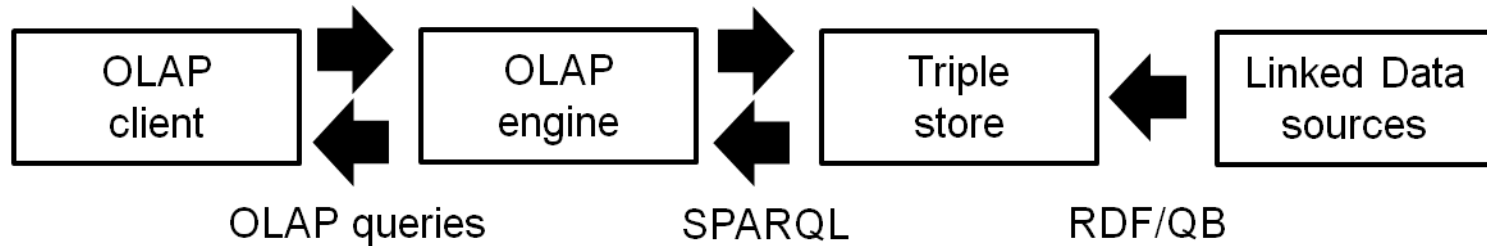
## OLAP query could be faster

- Data from the data cube is queried on demand, and no materialisation is done.
- No dice without slice; unnecessary computation of facts.
- No direct correspondence of SPARQL result and requested pivot table: Populating pivot table requires join.

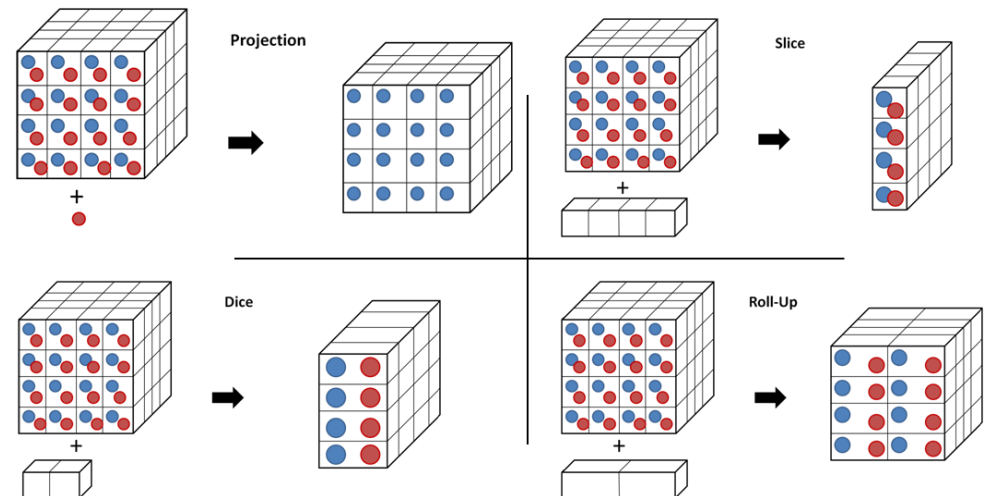
# Conclusions

- First work on OLAP-to-SPARQL mapping
  
- Future work
  - Investigating intuitive user interactions for navigating Data Cubes as Linked Data.
  - Considering OLAP hierarchies and multi-cube operations (e.g., Drill-Across).
  - Implementing an OLAP engine (olap4ld) for optimising OLAP query execution.

# Thanks!



Feedback?  
Questions?



More about OLAP of Linked Data: [http://semanticweb.org/wiki/OLAP\\_of\\_Linked\\_Data](http://semanticweb.org/wiki/OLAP_of_Linked_Data)



# References

- [1] Harth A. VisiNav : Visual Web Data Search and Navigation. In: *DEXA 2009*; 2009:214-228.
- [2] Aasman J, Cheetham K. RDF Browser for Data Discovery and Visual Query Building. *Interfaces*. 2011:1-4.
- [3] Kobilarov G, Dickinson I. Humboldt : Exploring Linked Data. *LDOW*. 2008.
- [4] The RDF Data Cube Vocabulary: <http://www.w3.org/TR/vocab-data-cube/>
- [5] Gray, J., Bosworth, a., Lyaman, a., Pirahesh, H.: Data cube: a relational aggregation operator generalizing GROUP-BY, CROSS-TAB, and SUB-TOTALS. Proceedings of the Twelfth International Conference on Data Engineering pp. 152-159 (1995)

# Backup: Multidimensional Model in RDF

**Member** defines the set of members as  $Member = \{?x \in (\mathcal{I} \cup \mathcal{B}) | (?x \text{ a } skos:Concept)\}$ . Let  $\mathcal{V} = 2^{Member}$ ,  $V \in \mathcal{V}$ ,  $ROLLUPMEMBER \subseteq Member \times Member$ ,  $rollupmember(V) = \{(v_1, v_2) \in V \times V | (iri(v_1) \text{ skos:broader } iri(v_2) \vee iri(v_2) \text{ skos:narrower } iri(v_1))\}$

**Level** defines the set of levels as  $Level = \{(?x, V, rollupmember(V)) \in (\mathcal{I} \cup \mathcal{B}) \times \mathcal{V} \times ROLLUPMEMBER | (?x \text{ a } skosclass:ClassificationLevel \wedge \forall v \in V(iri(v) \text{ skos:member } ?x))\}$ . Let  $\mathcal{L} = 2^{Level}$ ,  $L \in \mathcal{L}$ ,  $ROLLUPEVEL \subseteq Level \times Level$ ,  $rolluplevel(L) = \{(l_1, l_2) \in L \times L | (iri(l_1) \text{ skosclass:depth } x) \wedge (iri(l_2) \text{ skosclass:depth } y) \wedge x \leq y)\}$

**Hierarchy** defines the set of hierarchies as  $Hierarchy = \{(?x, L, rolluplevel(L)) \in (\mathcal{I} \cup \mathcal{B}) \times \mathcal{L} \times ROLLUPEVEL | (?x \text{ a } skos:ConceptScheme) \wedge \forall l \in L(iri(l) \text{ skos:inScheme } ?x)\}$ . Let  $\mathcal{H} = 2^{Hierarchy}$ .

**Dimension** defines the set of dimensions as  $Dimension = \{(?x, H) \in (\mathcal{I} \cup \mathcal{B}) \times \mathcal{H} | (?x \text{ a } qb:DimensionProperty) \wedge \forall h \in H(?x \text{ qb:codeList } iri(h))\}$ . Let  $\mathcal{D} = 2^{Dimension}$ .

**Measure** defines the set of measures as  $Measure = \{(?x, aggr) \in (\mathcal{I} \cup \mathcal{B}) \times \{UDF\} | (?x \text{ a } qb:MeasureProperty)\}$  with  $UDF$  a default aggregation function since QB so far does not provide a standard way to represent typical aggregation functions such as SUM, AVG and COUNT: if only one value is given, the value itself else the number of values is returned. Conceptually, measures are treated as members of a dimension-hierarchy-level combination labelled “Measures”. Let  $\mathcal{M} = 2^{Measure}$ .

# Backup: Dice = Slice + Filter

- Given the query model, a dice + slice cannot be represented, therefore dice = slice + filter.

## Scenario

$Q = (?, ?, ?, \text{ALL}, \text{Cost of goods sold}) \neq$   
 $(\{\text{RAYONIER INC}, \text{WEYERHAUSER CO}\}, ?, ?, \text{ALL}, \text{Cost of goods sold})$

Columns (issuer)		RAYONIER INC	WEYERHAEUSER CO	...	...
Rows (dtstart, dtend)				...	...
2009-01-01	2009-3-31	1,100,335 USD	0 values	...	...
2009-04-01	2009-06-30	2 values	2,300,800 USD	...	...
...	...	...	...	...	...

Filters: CostOfGoodsSold